# EVIDENCE OF AN UPPER BOUND ON THE MASSES OF PLANETS AND ITS IMPLICATIONS FOR GIANT PLANET FORMATION 

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#### Abstract

Celestial bodies with a mass of $M \approx 10 M_{\text {Jup }}$ have been found orbiting nearby stars. It is unknown whether these objects formed like gas-giant planets through core accretion or like stars through gravitational instability. I show that objects with $M \lesssim 4 M_{\text {Jup }}$ orbit metal-rich solar-type dwarf stars, a property associated with core accretion. Objects with $M \gtrsim 10 M_{\text {Jup }}$ do not share this property. This transition is coincident with a minimum in the occurrence rate of such objects, suggesting that the maximum mass of a celestial body formed through core accretion like a planet is less than $10 M_{\text {Jup }}$. Consequently, objects with $M \gtrsim 10 M_{\text {Jup }}$ orbiting solar-type dwarf stars likely formed through gravitational instability and should not be thought of as planets. Theoretical models of giant planet formation in scaled minimum-mass solar nebula Shakura-Sunyaev disks with standard parameters tuned to produce giant planets predict a maximum mass nearly an order of magnitude larger. To prevent newly formed giant planets from growing larger than $10 M_{\text {Jup }}$, protoplanetary disks must therefore be significantly less viscous or of lower mass than typically assumed during the runaway gas accretion stage of giant planet formation. Either effect would act to slow the Type I/II migration of planetary embryos/giant planets and promote their survival. These inferences are insensitive to the host star mass, planet formation location, or characteristic disk dissipation time.


Keywords: binaries: spectroscopic - brown dwarfs - planets and satellites: formation - protoplanetary disks - stars: formation - stars: low-mass

## 1. INTRODUCTION

Celestial bodies with a mass of $M \approx 10 M_{\text {Jup }}$ have been found orbiting nearby stars as well as floating freely in star-forming regions and the field (e.g., Latham et al. 1989; Zapatero Osorio et al. 2000; Kirkpatrick et al. 2006). Since it is currently impossible to determine the origin of a given $10 M_{\text {Jup }}$ object, it is unknown whether these bodies formed like gas-giant planets through core accretion or like stars through gravitational instability. If it were practical to infer the typical mass separating objects formed through core accretion from those formed through gravitational instability, it would be possible to derive otherwise unobtainable constraints on planet formation models as well as the structure and properties of planet-forming disks (e.g., Tanigawa \& Ikoma 2007; Tanigawa \& Tanaka 2016).
The existence of $10 M_{\text {Jup }}$ objects both in orbit around stars and in isolation, combined with the ambiguity of their formation, has made it difficult to define a clear mass upper limit for planets. The IAU Working Group on Extrasolar Planets adopted the working definition of a planet as an object with a true mass below the limiting mass for thermonuclear fusion of deuterium that orbits a star or stellar remnant. On the other hand, substellar objects with true masses above the limiting mass for thermonuclear fusion of deuterium were defined as brown dwarfs, regardless of how they formed or where they are located (Boss et al. 2007). At solar composition, the minimum mass to significantly burn deuterium is thought to be near $13 M_{\text {Jup }}$ independent of the formation channel (e.g., Grossman \& Graboske 1973; Saumon et al. 1996; Burrows et al. 1997; Spiegel et al. 2011; Bodenheimer et al. 2013). Other definitions for giant planets referencing their intrinsic properties have also been proposed (e.g., Hatzes \& Rauer 2015).

The definition of planets as objects with $M \lesssim 13 M_{\text {Jup }}$ is problematic for several reasons. The critical mass for deuterium burning is not a step function, so it is also necessary to arbitrarily specify the fraction of the initial deuterium burned to uniquely define the critical mass. Since the critical mass depends on the composition, at $M \approx 13 M_{\text {Jup }}$ a metal-poor object would be a planet while a metal-rich object would be a brown dwarf. Because the mass required for deuterium fusion depends on the internal properties of an object, its calculation is necessarily dependent on imperfect models. Finally, the definition does not take into account the potentially unique ways such objects are formed.

The elegance of a formation-based planet definition has been broadly recognized (e.g., Schneider et al. 2011; Wright et al. 2011; Chabrier et al. 2014). Under a formation-based definition, planets are celestial bodies
that form through core accretion (Pollack et al. 1996; Hubickyj et al. 2005). Conversely, brown dwarfs and stars form through direct gravitational collapse, either at the disk or core scale (e.g., Adams et al. 1989; Bate et al. 2003; Bate 2012; Kratter \& Lodato 2016). Despite the appeal of this definition, it has not been put into practice because of the difficulty in observationally determining the origin of individual celestial bodies orbiting distant stars.

Celestial bodies that form through core accretion and gravitational instability can be separated statistically though. Giant planets with a mass of $M \sim 1 M_{\text {Jup }}$ preferentially orbit dwarf stars that are metal rich. This fact is thought to be indicative of formation through core accretion (Santos et al. 2004; Fischer \& Valenti 2005; Sozzetti et al. 2006, 2009). This observational inference is supported by theoretical exoplanet population synthesis calculations, which suggest that the most massive objects formed through core accretion should be exclusively found around the most metal-rich stars (Mordasini et al. 2012). In contrast, gravitational instability is thought to occur with equal efficiency regardless of gas-phase metallicity (Boss 2002; Bate 2014). In accord with this idea, the occurrence of low-mass stars with $M \sim 100 M_{\text {Jup }}$ orbiting more massive stars like planets is independent of metal abundance (Latham et al. 2002; Carney et al. 2003). The maximum mass at which celestial bodies no longer preferentially orbit metal-rich solar-type dwarf stars can therefore be used to separate massive planets from brown dwarfs and establish the mass of the largest objects that can be formed through core accretion.
It has been impossible to confidently make this statistical separation in the past due to the lack of giant planets and brown dwarfs with mass estimates unaffected by the Doppler $\sin i$ degeneracy orbiting solar-type dwarf stars with homogeneous stellar parameters. That comparison is now possible. In this paper, I calculate the mass at which transiting objects no longer preferentially orbit metal-rich solar-type dwarf stars. The transition occurs somewhere in the range of $4 M_{\text {Jup }} \lesssim M \lesssim$ $10 M_{\text {Jup }}$, suggesting that objects with $M \lesssim 10 M_{\text {Jup }}$ form through core accretion like giant planets, while objects with $M \gtrsim 10 M_{\text {Jup }}$ form like stars through gravitational instability. I describe my sample definition in Section 2. I detail my analysis procedures and compare my results to a model of the runaway gas accretion stage of giant planet formation in Section 3. I discuss the overall results and implications in Section 4 and conclude by summarizing my findings in Section 5.

## 2. SAMPLE DEFINITION

I would like to calculate the mass at which secondary companions (e.g., planets, brown dwarfs, and low-mass stars) no longer preferentially orbit metal-rich solar-type dwarf primaries. I target systems where the minimum mass, $M_{2} \sin i$, of the secondary has been inferred with the Doppler technique and the inclination, $i$, of the orbit is known to be close to $90^{\circ}$ because of the observed transit. That has two major advantages. First, the minimum mass inferred for the secondary in each system from the Doppler measurement is very close to the true secondary mass because the observed transit ensures that $i \approx 90^{\circ} \Rightarrow \sin i \approx 1$. Second, the observation of both the Doppler and transit signals virtually guarantees that the secondary is real and not a false positive.

Using the application programming interface (API) call in Appendix A, I select from the NASA Exoplanet Archive all of the confirmed low-mass secondaries that have $M_{2} \geq 0.1 M_{\text {Jup }}$ and have been detected with both the Doppler and transit techniques. I cross match that sample on R.A. and decl. with the catalog of homogeneously derived exoplanet host star stellar parameters from SWEET-Cat (Santos et al. 2013; Andreasen et al. 2017). Though I did not explicitly restrict the sample to solar-type dwarf primaries, the requirements imposed above produce a sample of primary stars with $4500 \mathrm{~K} \lesssim T_{\text {eff }} \lesssim 7000 \mathrm{~K}$ and $\log g \gtrsim 4.0$. I rescale all of the secondary masses from the NASA Exoplanet Archive sample using the uniformly calculated SWEET-Cat primary star mass scale. I include in Table 1 the secondary masses and primary metallicities of the resulting sample of 119 systems. Because of the transit requirement, $95 \%$ of the objects in Table 1 have an orbital period of $P<10$ days and therefore a semimajor axis of $a \lesssim 0.1$ AU.

I compile from the literature a sample of brown dwarf and low-mass star secondaries with $M_{2} \lesssim 300 M_{\text {Jup }} \approx$ $0.30 M_{\odot}$ that have Doppler-inferred masses and that transit solar-type dwarf primaries. I include in Table 2 the secondary masses and primary metallicities of the resulting sample of 27 systems. Because of the transit requirement, $95 \%$ of the objects in Table 2 have $P<50$ days and therefore $a \lesssim 0.25 \mathrm{AU}$. This combined sample of 146 giant planets, brown dwarfs, and low-mass stars that have Doppler-inferred masses and transit solar-type primaries (most with homogeneously derived stellar parameters) is the best sample available to calculate the mass at which low-mass secondary companions no longer preferentially orbit metal-rich solar-type primaries.
Selection effects are unlikely to be present in this sample. In a signal-to-noise limited transit survey at a given period the number of systems discovered, $N$ scales as $N \propto R_{1}^{-7 / 2} R_{2}^{6}$, where $R_{1}$ is primary radius and $R_{2}$ is the
secondary radius (Pepper et al. 2003). All of the brown dwarfs and low-mass stars as well as almost all of the giant planets in this sample were discovered with the transit technique. They all orbit solar-type host stars with similar radii, so $R_{1} \approx 1 R_{\odot}$ for all 146 systems in the sample considered here. Because giant planets and brown dwarfs are both significantly supported by degeneracy pressure, radius is a weak function of mass in the interval of $1 M_{\text {Jup }} \lesssim M \lesssim 80 M_{\text {Jup }}$ (e.g., Zapolsky \& Salpeter 1969; Burrows \& Liebert 1993). Consequently, all 146 systems in this sample have $R_{2} \approx 1 R_{\text {Jup }}$. The Doppler technique can easily detect the orbital motion of the primary in all 146 systems in this sample, so it can be used to estimate the mass of the secondary in each system. For these reasons, transit surveys are equally complete for objects across the mass range of this sample.

Even though the period distribution of the transiting secondaries in this sample is biased toward short periods, that bias will not affect my goal of calculating the mass at which secondary companions no longer preferentially orbit metal-rich solar-type dwarf primaries. Both the preference of giant planets for metal-rich primaries and the indifference of low-mass stars to primary metallicity are independent of the period: Fischer \& Valenti (2005) showed that giant planets preferentially orbit metal-rich stars at all periods while Latham et al. (2002) demonstrated that the occurrence and period distributions of metal-poor and metal-rich binary systems are indistinguishable. Accordingly, there is no reason to believe that a similar analysis on a sample of the more common intermediate-period secondaries would produce a qualitatively different conclusion.

## 3. ANALYSIS

With the goal of identifying the mass at which lowmass secondaries no longer preferentially orbit solartype dwarf primaries, I analyze the 146 systems in Tables 1 and 2 in two independent ways. First, I apply clustering algorithms to the data in the $\log _{10}$ (secondary mass)-primary metallicity plane. Since each secondary formed either through core accretion or gravitational instability, I specify in advance that each algorithm should put each secondary in one of two clusters. The mass that forms the border between the two clusters is the mass at which secondaries no longer preferentially occur around metal-rich solar-type dwarf stars, which I interpret as the maximum mass of celestial bodies that form like planets through core accretion. Second, I take advantage of the theoretical prediction of Mordasini et al. (2012) that massive objects formed by core accretion should only occur around the most metal-rich primaries.

To that end, I calculate the median metallicity of the sample as a function of secondary mass in a kernel of constant width. I interpret the point at which the moving median metallicity drops below the smallest value seen in the planet mass range as the maximum mass of objects that form like planets, as massive objects formed by core accretion should orbit stars more metal-rich than that of the typical giant planet-host star. I detail these analyses in the following two subsections. I then use a semi-analytic model of the runaway gas accretion stage of giant planet formation to interpret the results in the last subsection.

### 3.1. Clustering Analysis

I use clustering algorithms from each of three classical clustering paradigms that span the space of modern clustering approaches: connectivity-based hierarchical clustering (Murtagh 1985), centroid-based $k$-means clustering (Hartigan \& Wong 1979), and distribution-based Gaussian-model clustering (Fraley \& Raftery 2002; Fraley et al. 2012; Schlaufman 2015). I summarize the key aspects of each algorithm below and provide the details in Appendix B.

The hierarchical clustering algorithm seeks to identify the maximally connected subgraph of a set of objects. It starts with a matrix of dissimilarity between all objects in a set. It then identifies the pair of objects with the smallest dissimilarity, combines them, and updates the dissimilarity of all remaining objects in the set with the minimum dissimilarity to either of the combined objects. It continues this process until only two objects remain. This algorithm requires the specification of a dissimilarity metric, and I use the Euclidean distance between each object.

The $k$-means clustering algorithm seeks to minimize the total dissimilarity between the ensemble of objects in each cluster and the cluster center. It starts by randomly placing a set of cluster centers in the space defined by the objects to be clustered. It then identifies the closest cluster center to each object and assigns that object to that cluster. The mean value of the ensemble of objects in each cluster is then set to be that cluster's center on the next iteration. The process continues until the movement of cluster centers on each update step is small. This algorithm requires the specification of a dissimilarity metric, and I use the Euclidean distance between each object.

The Gaussian-model clustering algorithm seeks to identify the mixture of Gaussians that has the highest likelihood of having generated the objects to be clustered. It starts by randomly choosing the mean and variance of each Gaussian as well as the contribution
of each Gaussian to the mixture. It then calculates the probability that each observation was produced by one component of the mixture. The object is assigned to the component most likely to have generated it and the mean and variance of each component are estimated based on the objects assigned to it. The proportion of each component is the fraction of objects assigned to it. This process is repeated until the change in model parameters is small.
To account for the observational uncertainty in each secondary mass and primary metallicity, I use a Monte Carlo simulation. First, I generate $10^{3}+1$ realizations of each secondary mass and primary metallicity from the observational uncertainties on those quantities and then apply all three clustering algorithms to each realization. For each algorithm, I aggregate the classifications across all iterations and assign to each system the most frequently determined classification. The final classification of each system is then the majority classification among the three different algorithms. I plot the result of this calculation in Figure 1. All systems with a secondary mass of $M_{2}<4 M_{\text {Jup }}$ are unanimously classified with giant planets, while all systems with a secondary mass of $M_{2}>10 M_{\text {Jup }}$ are unanimously classified with low-mass stars. A two-sample Kolmogorov-Smirnov test on the overall sample split at $M_{2}=10 M_{\text {Jup }}$ shows that the chance that the two metallicity distributions were produced by the same parent distribution is only $p=4.45 \times 10^{-3}$, or about $3.3 \sigma .{ }^{1}$

### 3.2. Moving Median Analysis

The clustering analysis described above implicitly makes use of the relative occurrence rates of giant planets, brown dwarfs, and low-mass stars. An alternative approach that does not implicitly use the occurrence rate is to calculate the median metallicity as a function of secondary mass in a kernel of a constant width. Since celestial bodies with $M \gtrsim 10 M_{\text {Jup }}$ formed via core accretion are thought to occur only around the most metal-rich stars (Mordasini et al. 2012), the mass at which the moving median metallicity moves below the lowest moving median metallicity observed in the giant planet region should also correspond to the maximum mass of the objects formed by core accretion.

To account for the observational uncertainty in each secondary mass and primary metallicity, I use a Monte Carlo simulation. First, I generate $10^{3}+1$ realizations

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Figure 1. Secondary mass-primary metallicity distribution for giant planets, brown dwarfs, and low-mass stars that transit solar-type dwarf stars. Objects classified unanimously by all three of the clustering paradigms are plotted as solid symbols, with circles for planets and squares for low-mass stars. Objects with classes agreed upon by two of the three clustering paradigms are plotted as open symbols, with circles for planets and squares for low-mass stars. The gray shading separates the unanimous classification regions. The black dashed line is the midpoint of the gray region. The blue and green regions are the bestfit two-component Gaussian mixture model, while the black cross in the lower right corner of the plot indicates the typical uncertainty.
of each secondary mass and primary metallicity from the observational uncertainties on those quantities and then calculate the moving median metallicity of each sample as a function of mass. I use a kernel of width $n=23$ objects, as this is the highest mass resolution that permits the measurement of the median metallicity with a similar precision as for the individual metallicity estimates $\left(\sigma_{[\mathrm{Fe} / \mathrm{H}]} \approx 0.05\right.$ dex $)$. I plot this result in Figure 2. Again, the point at which secondaries no longer preferentially orbit metal-rich solar-type dwarf-star primaries occurs at $M_{2} \approx 10 M_{\text {Jup }}$. This result is similar for all kernel widths that permit the measurement of the median metallicity with a similar precision as for the individual metallicity estimates.

### 3.3. Parameter Study of the Last Stage of Giant Planet Formation

The results in Sections 3.1 and 3.2 show that lowmass secondaries no longer preferentially orbit metalrich solar-type dwarf stars when $M_{2} \gtrsim 10 M_{\text {Jup }}$. Those
inferences support the idea that the most massive objects formed around solar-type stars like planets through core accretion have $M \approx 10 M_{\text {Jup }}$. I now use that inference to quantify the range of protoplanetary disk properties that could be expected to reproduce this result using the semi-analytic model of Tanigawa \& Tanaka (2016).

Tanigawa \& Tanaka (2016) modeled the last stage of giant planet formation (runaway envelope accretion) in a globally evolving protoplanetary disk using the Shakura \& Sunyaev (1973) model for disk viscosity and a selfsimilar solution for the disk's global evolution (e.g., Lynden-Bell \& Pringle 1974; Hartmann et al. 1998). The key parameters of the model are as follows:

1. The location of planet formation, $a_{p}$.
2. The disk viscosity, $\nu=\alpha c h$, where $\alpha$ is a unitless parameter independent of radius and time, $c$ is the sound speed of disk gas, and $h$ is the disk scale height.


Figure 2. Moving median metallicity as a function of secondary mass. The black line is the median metallicity in a kernel of width $n=23$ centered on the given mass. The gray region is the $1 \sigma$ uncertainty in the moving median. The blue rectangle indicates the range of median metallicity observed in the giant planet region. The green rectangle shows the range in mass where the moving median is below that seen in the giant planet region (i.e., $M \lesssim 4 M_{\text {Jup }}$ ). The boundary is near $10 M_{\text {Jup }}$.
3. The initial mass of the disk, $M_{\text {disk }}$, is assumed to scale linearly with a host star mass, $M_{*}$ and overall normalization, $f_{\Sigma}$. Here $f_{\Sigma}=1$ corresponds to the minimum-mass solar nebula of Hayashi et al. (1985).
4. The characteristic exponential disk depletion time, $\tau_{\text {dep }}$.

The model is informed by the latest numerical results showing that gaps cleared by giant planets are much shallower than previously thought (e.g., Duffell \& MacFadyen 2013; Fung et al. 2014). The model does not account for possible photoevaporation of disk gas due to far-ultraviolet radiation (e.g., Gorti et al. 2009), as the rate of mass loss expected is still uncertain by more than an order of magnitude (e.g., Alexander et al. 2014).

I have implemented the Tanigawa \& Tanaka (2016) model and used it to conduct a parameter study of the relationship between the maximum attainable mass of a giant planet and the model parameters $a_{p}, \alpha, M_{*}, f_{\Sigma}$, and $\tau_{\text {dep }}$. If not otherwise indicated, I assume that $a_{p}$ $=1 \mathrm{au}, M_{*}=1 M_{\odot}, \tau_{\text {dep }}=3 \times 10^{6} \mathrm{yr}$, the initial disk radius is $R_{0}=200 \mathrm{AU}$, and the seed embryo mass is $M_{\text {embryo }}=10 M_{\oplus}$. I plot the result in Figure 3. According to the model, a maximum giant planet mass in the range of $4 M_{\text {Jup }} \lesssim M \lesssim 10 M_{\text {Jup }}$ can be accommo-
dated only in a narrow corridor of the $\alpha-f_{\Sigma}$ plane from $\alpha \sim 10^{-4}$ and $f_{\Sigma} \sim 10^{0.5}$ to $\alpha \sim 10^{-2}$ and $f_{\Sigma} \sim 10^{-1}$. This result is only weakly dependent on the mass of the primary star, the location of planet formation, or the disk depletion time. These results are unique in that they indirectly constrain the viscosities and masses of long since dissipated disks during their epoch of giant planet formation.

## 4. DISCUSSION

I have shown that celestial bodies with $M \lesssim 10 M_{\text {Jup }}$ orbit metal-rich solar-type dwarf stars, a property thought to indicate formation through core accretion (e.g., Santos et al. 2004; Fischer \& Valenti 2005). On the other hand, celestial bodies with $M \gtrsim 10 M_{\text {Jup }}$ do not preferentially orbit metal-rich stars, so there is no reason to believe that they form through core accretion. Since gravitational instability is thought to be independent of metallicity (e.g., Boss 2002), it can easily accommodate this observation.

This boundary at $M \approx 10 M_{\text {Jup }}$ between objects formed via core accretion and gravitational instability is coincident with a minimum in the occurrence rate of companions to solar-type dwarf stars with $P<100$ days as a function of minimum mass. I plot the occurrence rate of giant planets, brown dwarfs, and low-mass stars discovered with the Doppler technique in Figure 4. The observation that the upper limit on the mass of giant planets identified by the clustering analysis occurs at the minimum in the occurrence rate of celestial bodies orbiting solar-type dwarf stars supports the idea that core accretion does not generally form objects with $M \gtrsim 10 M_{\text {Jup }}$.

This boundary at $M \approx 10 M_{\text {Jup }}$ between objects formed via core accretion and gravitational instability is also supported by interior models for three massive objects that straddle the boundary: HAT-P-20 b ( $M \approx 7.3 M_{\text {Jup }}$ - Bakos et al. 2011), HAT-P-2 b ( $M \approx 9.0 M_{\text {Jup }}$ - Bakos et al. 2007a), and Kepler$75 \mathrm{~b}\left(M \approx 10.1 M_{\mathrm{Jup}}\right.$ - Bonomo et al. 2015). Interior models indicate HAT-P-20 b and HAT-P-2 b have large amounts of heavy elements as expected if they formed through core accretion, while Kepler-75 b is consistent with the composition of its host star as expected if it formed through gravitational instability (Leconte et al. 2009; Thorngren et al. 2016).

### 4.1. Implications for Planet Formation

The results presented in Section 3 indicate that a $M \approx 10 M_{\text {Jup }}$ maximum mass for objects formed by core accretion can only be accommodated in a narrow band in the Shakura \& Sunyaev (1973) viscosity parameter $\alpha$-minimum-mass solar nebular scaling factor $f_{\Sigma}$


Figure 3. Maximum mass attainable by a giant planet formed by core accretion according the model of Tanigawa \& Tanaka (2016) as a function of the viscosity parameter $\alpha$ of Shakura \& Sunyaev (1973) and minimum-mass solar nebular scaling factor, $f_{\Sigma}$. Dark colors are indicative of high-mass planets, while lighter colors are indicative of low-mass planets. The labeled contours delimit the region of maximum mass permitted by the analyses presented in Sections 3.1 and 3.2. The top row varies the host star mass, $M_{*}$, the middle row varies the location of planet formation, $a_{p}$, and the bottom row varies the characteristic disk depletion time, $\tau_{\text {dep }}$.


Figure 4. Secondary occurrence rate as a function of secondary minimum mass at $P<100$ days. The secondary occurrence rate in the range of $0.1 M_{\text {Jup }}<M \sin i<15 M_{\text {Jup }}$ is from Cumming et al. (2008), while the occurrence rate in the range of $15 M_{\text {Jup }}<M \sin i<100 M_{\text {Jup }}$ is from Troup et al. (2016). The gray shading and black dashed line are the same as in Figure 1. They separate the regions identified by the clustering analysis.
plane from $\alpha \sim 10^{-4}$ and $f_{\Sigma} \sim 10^{0.5}$ to $\alpha \sim 10^{-2}$ and $f_{\Sigma} \sim 10^{-1}$. Observations of T Tauri stars have been used to suggest that protoplanetary disks can be well reproduced by models with $\alpha \sim 10^{-2}$ (e.g., Hartmann et al. 1998). At the same time, classical models of giant planet formation though core accretion almost always invoke disks several times more massive than that of the minimum-mass solar nebula-or $f_{\Sigma} \gtrsim 3$ - to ensure core formation before disk dissipation (e.g., Pollack et al. 1996; Ikoma et al. 2000; Alibert et al. 2005; Hubickyj et al. 2005; Lissauer et al. 2009; Movshovitz et al. 2010; D'Angelo et al. 2014). In a disk with $\alpha=10^{-2}$ and $f_{\Sigma}=3$, the Tanigawa \& Tanaka (2016) model predicts a giant planet maximum mass of $M \approx 60 M_{\mathrm{Jup}}$. According to these results, either but not both, of these traditional assumptions could be made during the runaway gas accretion stage of giant planet formation.

If the $M \approx 10 M_{\text {Jup }}$ threshold is the result of lowviscosity or low-mass disks, then it would provide solutions to the long-standing Type I and Type II migration problems. Type I migration occurs when planetary embryos with $M_{\text {embryo }} \sim 1 M_{\oplus}$ that are not massive enough to open a gap in their parent protoplanetary disks lose angular momentum and move inward due to net negative torques from the disk. Though the processes responsible are complex and no model is yet completely satisfactory, the simplest models suggest that the
timescale for migration is very fast (e.g., Ward 1997; Tanaka et al. 2002). Exoplanet population synthesis calculations assuming fast Type I migration are unable to reproduce the existence of planets with $M \gtrsim 10 M_{\oplus}$ and $P \gtrsim 10$ days, so Type I migration must be slower than the simplest calculations initially suggested (e.g., Ida \& Lin 2008; Schlaufman et al. 2009). While many solutions have been proposed, ${ }^{2}$ it has been shown that Type I migration in disks with $\alpha \sim 10^{-4}$ is sufficiently slow that planetary embryos will survive and potentially grow into giant planets (e.g., Rafikov 2002; Li et al. 2009). Similarly, in disks with $\alpha \sim 10^{-2}$, the Type I migration rate is thought to be linearly dependent on disk surface density (e.g., Baruteau et al. 2016). A minimum-mass solar nebular scaling factor of $f_{\Sigma} \sim 10^{-1}$ would reduce the Type I migration rate by an order of magnitude, exactly the amount needed to reproduce the observed distribution of exoplanet properties in population synthesis calculations (e.g., Ida \& Lin 2008; Schlaufman et al. 2009).

Low-viscosity or low-mass disks would also solve the Type II migration problem. Type II migration occurs when planets that are massive enough to open a gap in their parent protoplanetary disks are carried into the close proximity of their host star on the disk viscous time (Lin et al. 1996), possibly precluding the existence of long-period giant planets. In disks where the mass of the disk locally dominates the mass of the planet, the Type II migration rate is inversely proportional to the viscosity (e.g., Lin et al. 1996; Tanigawa \& Tanaka 2016). Similarly, in a low-mass disk where the mass of the planet locally dominates the mass of the disk, the Type II migration rate is inversely proportional to the disk mass (e.g., Duffell et al. 2014). Consequently, low-viscosity or low-mass disks promote the existence of long-period giant planets.

Though these results were derived strictly for solartype dwarf stars with short-period transiting companions, the analysis in Section 3.3 suggests that the inference about planet formation is not strongly dependent on host-star mass, planet-formation location, or disk dissipation timescale. Indeed, similar inferences have been made using the much-more distant solar system giant planets Jupiter and Saturn by Lissauer et al. (2009) and Tanigawa \& Tanaka (2016). It is also reassuring that this upper limit of $10 M_{\mathrm{Jup}}$ on the mass of planets within 1 au of their host stars is consistent with the most advanced exoplanet population synthesis calculations currently available (Ida et al. 2013). Finally, support for

[^1]low-viscosity or low-mass disks as the origin of planetary systems has been found in many places from meteoritics in the solar system to super-Earths and mini-Neptunes in the Kepler field (e.g., Desch et al. 2017; Lee et al. 2017).

### 4.2. Comparison to Previous Studies of the Relationship between Giant Planets, Brown Dwarfs, and Host-star Properties

This study focused on giant planets, brown dwarfs, and low-mass stars with Doppler-inferred masses transiting solar-type dwarf stars with homogeneously estimated stellar parameters. It showed that low-mass secondaries with $M_{2}<10 M_{\text {Jup }}$ preferentially orbit metalrich stars, while secondaries with $M_{2}>10 M_{\text {Jup }}$ occur independent of host star metallicity. The difference between the metallicity distributions of objects in my sample with $M>10 M_{\text {Jup }}$ and $M<10 M_{\text {Jup }}$ is significant at more than $3.3 \sigma$, and this result cannot be attributed solely to the possible change in the occurrence rate of such bodies at $M \approx 4 M_{\text {Jup }}$. Since a preference for metal-rich host stars is thought to indicate formation through core accretion, these results suggest that the most massive objects that can be formed like planets through core accretion have $M \approx 10 M_{\text {Jup }}$.
Unlike all previous studies, these results are unaffected by the Doppler $\sin i$ degeneracy, the presence of possible false positives in the analysis sample, or the potentially weak or nonexistent giant planet-host star metallicity correlation for giant stars (e.g., Sadakane et al. 2005; Schuler et al. 2005; Hekker \& Meléndez 2007; Pasquini et al. 2007; Takeda et al. 2008; Ghezzi et al. 2010; Maldonado et al. 2013; Mortier et al. 2013a; Jofré et al. 2015; Reffert et al. 2015). Because of its large sample and use of $M$ instead of $M \sin i$, it has the best resolution in mass of all studies to date. All of these properties have enabled the identification of a difference between the metallicity distributions of objects with $M>10 M_{\text {Jup }}$ and $M<10 M_{\text {Jup }}$ at a higher statistical significance than any previous study of solar-type dwarfs. It is also the first study to couple its result to a detailed model of the runaway gas accretion stage of giant planet formation to constrain the properties of protoplanetary disks that are known to have formed giant planets.

The first studies seeking to compare giant planets and brown dwarfs to explore their origin all focused on the orbital properties of brown dwarfs. Grether \& Lineweaver (2006) examined the mass distribution of companions to solar-type stars with $P<5$ yr and determined that the minimum of the distribution occurs at $M \sin i=31_{-18}^{+25} M_{\text {Jup }}$. Because there was no such minimum in the mass spectrum of free-floating brown
dwarfs, they speculated that migration and not a characteristic mass scale of fragmentation in protoplanetary disks was responsible for the apparent minimum.

Sahlmann et al. (2011) used the combination of the Doppler and astrometric techniques to remove the $\sin i$ degeneracy to confirm the previous result, finding that low-mass brown dwarfs with $M \lesssim 25 M_{\text {Jup }}$ cleanly separated from high-mass brown dwarfs with $M \gtrsim 45 M_{\text {Jup }}$. In contrast to Grether \& Lineweaver (2006), they argued that the low-mass brown dwarfs may be massive planets formed by core accretion. They also showed that samples of brown dwarf candidates discovered solely by the Doppler technique with $M \sin i \gtrsim 45 M_{\text {Jup }}$ are significantly contaminated by inclined low-mass stars. ${ }^{3}$
Ma \& Ge (2014) extended these results by demonstrating that brown dwarfs with $M \sin i \lesssim 42.5 M_{\text {Jup }}$ and $M \sin i \gtrsim 42.5 M_{\text {Jup }}$ are unlikely to have the same eccentricity distribution at the $2.1 \sigma$ level. They suggested that the low-mass brown dwarfs formed by disk fragmentation, while the high-mass brown dwarfs formed by fragmentation at the core scale. They also showed that the giant planet and brown dwarf host stars were unlikely to have the same metallicity distribution at the $3.3 \sigma$ level. Selection effects in the giant planet-host sample and inclined low-mass star contamination in the brown dwarf sample likely affect these conclusions to some degree though.

More recent efforts to investigate the differences between massive planets and brown dwarfs have focused on host star metallicity and chemical abundance. Using a sample of solar-type dwarf stars unaffected by selection effects or inclined low-mass star contamination, Mata Sánchez et al. (2014) found that the metallicities and $\alpha$-element abundances of brown dwarf hosts are lower than the metallicities of giant planet-host stars at the $1.7 \sigma$ and $1.8 \sigma$ levels.
Maldonado \& Villaver (2017) presented a similar analysis to Ma \& Ge (2014) that used homogeneously derived stellar parameters to show that low-mass brown dwarf host are more metal-rich than high-mass brown dwarf hosts at the $2.4 \sigma$ level. However, the difference was not significant if only dwarf host stars were included or if a random distribution of inclination was assumed. The fact that the significance of their result is reduced when accounting for a random distribution of inclination suggests that low-mass stars on low-inclination orbits contaminated their sample. In addition, their compete sample of brown dwarf hosts was significantly more metal

[^2]poor than their sample of giant planet-host stars. At the same time, their low-mass brown dwarfs were consistent with having the same metallicity distribution as the giant planet-host stars, though their $\alpha$-element distributions differed at the $2.4 \sigma$ level.
Santos et al. (2017) studied the minimum-mass and metallicity distributions of mostly Doppler-discovered objects with $M \sin i<15 M_{\text {Jup }}, 10$ days $<P<$ 1825 days, and with homogeneous stellar parameters available in the SWEET-Cat database. Using both multivariate Gaussian modeling and KolmogorovSmirnov tests, they argued that planets below and above $M \sin i=4 M_{\text {Jup }}$ have distinct metallicity distributions and therefore distinct formation channels. In particular, they suggested that the giant planets with $M \sin i \lesssim 4 M_{\text {Jup }}$ formed via core accretion while the giant planets with $M \sin i \gtrsim 4 M_{\text {Jup }}$ formed via gravitational instability. Their multivariate Gaussian inference is mostly due to the apparent cutoff in the giant planet occurrence distribution at $M \sin i \approx 4 M_{\text {Jup }}$. In their Kolmogorov-Smirnov tests, the distributions were distinct at the $3.3 \sigma$ significance substantially because of the inclusion of giant stars with $M \gtrsim 1.5 M_{\odot}$. The fact that restricting the sample to solar-type dwarf stars reduced the significance of their inference to $1.6 \sigma$ indicates that either false positives in the giant star sample or the possibly diminished giant planet occurrence-host star metallicity effect for giant stars may play a role in the significant difference they identified in their sample including both dwarf and giant host stars. A critical mass of $M \sin i=4 M_{\text {Jup }}$ is also inconsistent with the heavy element enrichment observed in HAT-P-20 b and HAT-P-2 b. Nevertheless, my study confirms the hint identified in Santos et al. (2017) and presents the strongest evidence to date that the maximum mass of objects formed via core accretion is in the range of $4 M_{\text {Jup }} \lesssim M \lesssim 10 M_{\text {Jup }}$.

### 4.3. A Formation-based Definition for Planets

This analysis has shown that objects with $M \lesssim$ $10 M_{\text {Jup }}$ preferentially orbit metal-rich solar-type dwarf stars. That property has been suggested to be a natural outcome of the core accretion model of giant planet formation. On the other hand, objects with $M \gtrsim 10 M_{\text {Jup }}$ orbit stars spanning the whole range of the thin disk metallicity distribution. That property is shared with low-mass stars, which must have formed by some sort of gravitational instability.
I propose that planets be defined as objects that orbit stars or stellar remnants and have a true mass below the threshold at which low-mass companions no longer preferentially orbit metal-rich solar-type dwarf stars. The
analyses presented in Sections 3.1 and 3.2 suggest this threshold is at $M \approx 10 M_{\mathrm{Jup}}$, but future data may revise this estimate. This definition has the same form as the working definition adopted by the IAU Working Group on Extrasolar Planets, but the maximum mass is now referenced to the maximum mass of objects formed by core accretion. This definition does not require the specification of an arbitrarily amount of deuterium burning, and it does not depend on an object's metallicity. Additionally, it is independent of the uncertain internal structure of objects at this mass scale. Furthermore, I propose that substellar objects with true masses above the threshold be defined as brown dwarfs, regardless of where they are located.

### 4.4. Predictions for Future Gaia Observations

The results presented in Sections 3.1 and 3.2 lead to the prediction that planets with $1 M_{\text {Jup }} \lesssim M \lesssim$ $10 M_{\text {Jup }}$ should preferentially be found around metalrich solar-type dwarf stars. In contrast, brown dwarfs with $10 M_{\text {Jup }} \lesssim M \lesssim 80 M_{\text {Jup }}$ should be found around solar-type dwarf stars that span the metallicity range of the Milky Way's thin disk. This prediction will soon be tested at an unprecedented scale. By the end of its planned five-year mission, the European Space Agency's Gaia satellite is expected to discover astrometrically and characterize $21,000 \pm 6000$ giant planets and brown dwarfs with $1 M_{\text {Jup }}<M<15 M_{\text {Jup }}$ and $1 \mathrm{AU} \lesssim a \lesssim 5 \mathrm{AU}$ (Perryman et al. 2014). This sample of giant planet and brown dwarf mass measurements will be nearly 100 times larger than the sample currently available and extend to the more common intermediateperiod objects lacking in my sample. For these reasons, Gaia will provide the definitive test of this prediction that planets with $1 M_{\text {Jup }} \lesssim M \lesssim 10 M_{\text {Jup }}$ should preferentially be found around metal-rich solar-type dwarf stars, while brown dwarfs with $10 M_{\text {Jup }} \lesssim M \lesssim 80 M_{\text {Jup }}$ should be found around solar-type dwarf stars that span the metallicity range of the Milky Way's thin disk.

## 5. CONCLUSION

Celestial bodies with $M \lesssim 10 M_{\text {Jup }}$ preferentially orbit metal-rich solar-type dwarf stars, while celestial bodies with $M \gtrsim 10 M_{\text {Jup }}$ do not preferentially orbit metalrich solar-type dwarf stars. A preference for metalrich host stars is thought to be a property of objects formed like giant planets through core accretion, while objects formed like stars through gravitational instability should not prefer metal-rich primaries. As a result, these data suggest that core accretion rarely forms giant planets with $M \gtrsim 10 M_{\text {Jup }}$ and objects more massive than $M \approx 10 M_{\text {Jup }}$ should not be thought of as planets. Instead, objects with $M \gtrsim 10 M_{\text {Jup }}$ formed like
stars through gravitational instability. An upper limit of $M \approx 10 M_{\text {Jup }}$ to the mass of planets can only be accommodated in either low-viscosity or low-mass protoplanetary disks. In either case, both Type I and Type II migration are an order of magnitude slower than traditionally assumed. For that reason, these results may point toward the solution of both the Type I and Type II migration problems. Finally, these observations put the definition of a planet as a secondary with $M \lesssim 10 M_{\text {Jup }}$ formed via core accretion on a solid observational basis for the first time.
ments. This research has made use of NASA's Astrophysics Data System Bibliographic Services, the SIMBAD database, operated at CDS, Strasbourg, France (Wenger et al. 2000), and the NASA Exoplanet Archive, which is operated by the California Institute of Technology, under contract with the National Aeronautics and Space Administration under the Exoplanet Exploration Program.

Software: mclust (Fraley et al. 2012), R (R Core Team 2017), TOPCAT (Taylor 2005)

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## APPENDIX

## A. API CALL FOR SAMPLE SELECTION

The following URL can be used to reproduce my initial selection with the API available from the NASA Exoplanet Archive:

```
http://exoplanetarchive.ipac.caltech.edu/cgi-bin/nstedAPI/nph-nstedAPI?&table=exoplanets&select=pl_hostname,
    ra,dec,st_mass,st_masserr1,st_masserr2,st_metfe,st_metfeerr1,st_metfeerr2,pl_name,pl_letter,pl_bmassj,
    pl_bmassjerr1,pl_bmassjerr2,pl_massj,pl_massjerr1,pl_massjerr2,pl_disc_refname,pl_disc_reflink,
    pl_def_refname,pl_def_reflink&where=pl_tranflag=1 and pl_rvflag=1 and pl_massj>=0.1&order=pl_bmassj
```


## B. DETAILS OF CLUSTERING ALGORITHMS

## B.1. Hierarchical clustering

I use the hclust function in R for hierarchical clustering ( R Core Team 2017). That implementation follows the algorithm of Murtagh (1985):

1. Calculate the set of $n(n-1) / 2$ dissimilarities between $n$ objects.
2. Identify the smallest dissimilarity $d_{i k}$.
3. Combine objects $i$ and $k$. That is, replace the two objects with a new object, $i \bigcup k$, and update all other dissimilarities such that for all objects $j \neq i, k$ the dissimilarity $d_{i} \cup k, j=\min \left(d_{i, j}, d_{k, j}\right)$. Delete the dissimilarities $d_{i, j}$ and $d_{k, j}$.
4. Return to Step 2 while the number of objects remaining is greater than two.

This algorithm requires the specification of a dissimilarity metric, and I use the Euclidean distance between each object.

## B.2. $k$-means Clustering

I use the kmeans function in R for $k$-means clustering ( R Core Team 2017). That implementation follows the algorithm of Hartigan \& Wong (1979):

1. Pick $k$ objects from the $n$ objects to be clustered.
2. Assign each object to a cluster by placing each it in the cluster, $k_{i}$, that has the centroid with the smallest dissimilarity.
3. Recalculate the centroid of each cluster.
4. Return to Step 2, unless changes in the cluster centroids are small.

This algorithm requires the specification of a dissimilarity metric, and I use the Euclidean distance between each object.

## B.3. Gaussian-model Clustering

I use the mclust package in R for Gaussian-model clustering (Fraley et al. 2012; R Core Team 2017). The algorithm is considerably more complex than either the hierarchical or $k$-means algorithms, so the interested reader should see Fraley \& Raftery (2002) for the details of the algorithm.

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Table 1. Giant Planets and Brown Dwarfs that have Doppler-inferred Masses and Transit Solar-type Stars with Homogeneous Stellar Parameters from SWEET-Cat

Table 1 (continued)

| Table 1 (continued) |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| System | Simbad | R.A. | Decl. | Mass | Metallicity | Discovery | Stellar Parameter |  |
|  | Name |  |  |  |  | Reference | Reference |  |
|  |  | ( hms ) | ( dms ) | ( $M_{\text {Jup }}$ ) |  |  |  |  |
| WASP-35 | TYC 4762-714-1 | 050419.6327 | -06 1347.376 | $0.69_{-0.06}^{+0.06}$ | ${ }_{-0.05}+0.05$ | Enoch et al. (2011a) | Mortier et al. (2013b) |  |
| CoRoT-4 | Corot-4 | 064846.715 | -00 4021.98 | $0_{0.71}{ }_{-0.08}^{+0.08}$ | $0.15{ }_{-0.06}^{+0.06}$ | Aigrain et al. (2008) | Mortier et al. (2013b) |  |
| HAT-P-4 | BD+36 2593 | 151957.9275 | +361346.785 | $0.71{ }_{-0.05}^{+0.03}$ | $0.35_{-0.08}^{+0.08}$ | Kovács et al. (2007) | Ammler-von Eiff et al. (2009) |  |
| TrES-1 | NAME TrES-1b | 190409.844 | +36 3757.54 | $0.73{ }_{-0.04}^{+0.05}$ | $0.06{ }_{-0.05}^{+0.05}$ | Alonso et al. (2004) | Santos et al. (2006) |  |
| HAT-P-41 | TYC 488-2442-1 | 194917.4383 | +044020.763 | $0.75{ }_{-0.10}^{+0.10}$ | $0.13_{-0.05}^{+0.05}$ | Hartman et al. (2012) | Tsantaki et al. (2014) |  |
| CoRot-9 | CoRot-9 | 184308.810 | +061214.89 | $0.81{ }_{-0.07}^{+0.07}$ | ${ }_{-0.02}{ }_{-0.03}^{+0.03}$ | Deeg et al. (2010) | Mortier et al. (2013b) |  |
| Corot-12 | CoRot-12 | 064303.762 | -011747.12 | $0.85{ }_{-0.06}^{+0.07}$ | $0.17_{-0.14}^{+0.14}$ | Gillon et al. (2010) | Mortier et al. (2013b) |  |
| WASP-16 | TYC 6147-229-1 | 141843.922 | -20 1631.85 | $0.86{ }_{-0.08}^{+0.04}$ | $0.13_{-0.02}^{+0.02}$ | Lister et al. (2009) | Mortier et al. (2013b) |  |
| XO-1 | BD+28 2507 | 160211.8470 | +281010.421 | $0.86{ }_{-0.07}^{+0.07}$ | ${ }_{-0.01}{ }_{-0.05}^{+0.05}$ | McCullough et al. (2006) | Ammler-von Eiff et al. (2009) |  |
| WASP-1 | TYC 2265-107-1 | 002040.077 | +315923.79 | $0.87{ }_{-0.05}^{+0.06}$ | $0.23{ }_{-0.03}^{+0.03}$ | Collier Cameron et al. (2007) | Mortier et al. (2013b) |  |
| WASP-2 | WASP-2 | 203054.130 | +062546.37 | $0.87_{-0.09}^{+0.09}$ | $0.02{ }_{-0.05}^{+0.05}$ | Collier Cameron et al. (2007) | Mortier et al. (2013b) |  |
| WASP-76 | BD+01 316 | 014631.8590 | +02 4202.065 | $0.88{ }_{-0.03}^{+0.03}$ | $0.36{ }_{-0.04}^{+0.04}$ | West et al. (2016) | Andreasen et al. (2017) |  |
| WASP-23 | GSC 07635-01376 | 064430.65 | -42 4541.0 | $0.91{ }_{-0.10}^{+0.09}$ | $0.05{ }_{-0.06}^{+0.06}$ | Triaud et al. (2011) | Mortier et al. (2013b) |  |
| WASP-28 | 2MASS J23342787-0134482 | 233427.881 | -01 3448.13 | $0.91{ }_{-0.04}^{+0.04}$ | $-0.12{ }_{-0.03}^{+0.03}$ | Anderson et al. (2015) | Mortier et al. (2013b) |  |
| WASP-41 | TYC 7247-587-1 | 124228.497 | -30 3823.55 | $0.92{ }_{-0.05}^{+0.05}$ | $0.06{ }_{-0.02}^{+0.02}$ | Maxted et al. (2011) | Mortier et al. (2013b) |  |
| WASP-79 | CD-30 1812 | 042529.0162 | -30 3601.603 | $0_{0.92}{ }_{-0.08}^{+0.08}$ | $0.19_{-0.10}^{+0.10}$ | Smalley et al. (2012) | Mortier et al. (2013b) |  |
| WASP-78 | TYC 5889-271-1 | 041501.5044 | -22 0659.109 | $0.93{ }_{-0.08}^{+0.08}$ | $-0.07_{-0.05}^{+0.05}$ | Smalley et al. (2012) | Mortier et al. (2013b) | $\sim$ |
| WASP-7 | HD 197286 | 204410.2190 | -39 1330.894 | $0.95{ }_{-0.13}^{+0.13}$ | $0.12{ }_{-0.09}^{+0.09}$ | Hellier et al. (2009b) | Mortier et al. (2013b) | A |
| WASP-44 | GSC 05264-00740 | 001536.770 | -115617.30 | $0.96{ }_{-0.07}^{+0.07}$ | $0.17_{-0.06}^{+0.06}$ | Anderson et al. (2012) | Andreasen et al. (2017) |  |
| WASP-58 | TYC 3525-76-1 | 181848.2530 | +45 1019.257 | $0.98{ }_{-0.08}^{+0.08}$ | $-0.09_{-0.04}^{+0.04}$ | Hébrard et al. (2013) | Andreasen et al. (2017) | T |
| HAT-P-35 | TYC 203-1079-1 | 081300.1827 | +044713.382 | $1.01{ }_{-0.03}^{+0.03}$ | $0.12_{-0.03}^{+0.03}$ | Bakos et al. (2012) | Mortier et al. (2013b) | 3 |
| OGLE-TR-182 | OGLE-TR 182 | 110918.71 | -61 0542.9 | $1.01{ }_{-0.15}^{+0.15}$ | $0.37_{-0.08}^{+0.08}$ | Pont et al. (2008) | Pont et al. (2008) | z |
| OGLE-TR-211 | 2MASS J10401438-6227201 | 104014.39 | -62 2720.2 | $1.02{ }_{-0.20}^{+0.20}$ | $0.11_{-0.10}^{+0.10}$ | Udalski et al. (2008) | Udalski et al. (2008) |  |
| WASP-26 | TYC 5839-876-1 | 001824.7001 | -15 1602.287 | $1.02{ }_{-0.02}^{+0.02}$ | $0.16_{-0.02}^{+0.02}$ | Smalley et al. (2010) | Mortier et al. (2013b) |  |
| WASP-24 | TYC 339-329-1 | 150851.7355 | +02 2035.953 | $1.03_{-0.04}^{+0.03}$ | $0.09{ }_{-0.04}^{+0.04}$ | Street et al. (2010) | Mortier et al. (2013b) |  |
| HAT-P-6 | TYC 3239-992-1 | 233905.8108 | +422757.502 | $1.04{ }_{-0.12}^{+0.12}$ | $-0.08{ }_{-0.11}^{+0.11}$ | Noyes et al. (2008) | Ammler-von Eiff et al. (2009) |  |
| WASP-45 | TYC 6996-583-1 | 002056.9941 | -35 5953.756 | $1.04{ }_{-0.06}^{+0.06}$ | $0.43{ }_{-0.06}^{+0.06}$ | Anderson et al. (2012) | Mortier et al. (2013b) |  |
| HAT-P-42 | GSC 00232-01451 | 090122.648 | +06 0549.99 | $1.07{ }_{-0.09}^{+0.09}$ | $0.34{ }_{-0.05}^{+0.05}$ | Boisse et al. (2013) | Andreasen et al. (2017) |  |
| WASP-82 | TYC 88-57-1 | 045038.5600 | +0153 38.088 | $1.11_{-0.04}^{+0.04}$ | $0.18{ }_{-0.04}^{+0.04}$ | West et al. (2016) | Andreasen et al. (2017) |  |
| WASP-19 | GSC 08181-01711 | 095340.077 | -45 3933.06 | $1.13{ }_{-0.04}^{+0.04}$ | $0.26{ }_{-0.05}^{+0.05}$ | Hebb et al. (2010) | Mortier et al. (2013b) |  |
| WASP-75 | GSC 05816-01135 | 224932.568 | -10 4031.93 | $1.14{ }_{-0.05}^{+0.05}$ | $0.24{ }_{-0.03}^{+0.03}$ | Gómez Maqueo Chew et al. (2013) | Andreasen et al. (2017) |  |
| CoRot-1 | CoRot-1 | 064819.172 | -03 0607.68 | $1.16{ }_{-0.13}^{+0.13}$ | $0.03_{-0.04}^{+0.04}$ | Barge et al. (2008) | Mortier et al. (2013b) |  |
| OGLE-TR-132 | V* V742 Car | 105034.72 | -61 5725.9 | $1.16{ }_{-0.13}^{+0.14}$ | $0.37{ }_{-0.07}^{+0.07}$ | Bouchy et al. (2004) | Gillon et al. (2007) |  |
| WASP-95 | CD-48 14223 | 222949.7348 | -4800 11.012 | $1.16{ }_{-0.04}^{+0.10}$ | $0.22_{-0.03}^{+0.03}$ | Hellier et al. (2014) | Andreasen et al. (2017) |  |
| WASP-47 | EPIC 206103150 | 220448.731 | -120107.99 | $1.18{ }_{-0.38}^{+0.58}$ | $0.36{ }_{-0.05}^{+0.05}$ | Hellier et al. (2012) | Mortier et al. (2013b) |  |
| HD 189733 | HD 189733 | 200043.7128 | +22 4239.074 | $1.19{ }_{-0.06}^{+0.06}$ | ${ }_{0.03}{ }_{-0.08}^{+0.08}$ | Bouchy et al. (2005) | Mortier et al. (2013b) |  |
| WASP-4 | 2MASS J23341508-4203411 | 233415.082 | -42 0341.14 | $1.22{ }_{-0.01}^{+0.01}$ | $0.03{ }_{-0.03}^{+0.03}$ | Wilson et al. (2008) | Mortier et al. (2013b) |  |
| TrES-2 | Kepler-1b | 190714.035 | +491859.07 | $1.25{ }_{-0.07}^{+0.07}$ | $0.06{ }_{-0.08}^{+0.08}$ | O'Donovan et al. (2006) | Ammler-von Eiff et al. (2009) |  |
| OGLE-TR-113 | V* V752 Car | 105224.40 | -61 2648.5 | $1.26{ }_{-0.16}^{+0.16}$ | $0.03{ }_{-0.06}^{+0.06}$ | Bouchy et al. (2004) | Mortier et al. (2013b) |  |
| WASP-97 | CD-56 324 | 013825.0569 | -55 4619.511 | $1.33{ }_{-0.05}^{+0.05}$ | $0.31{ }_{-0.04}^{+0.04}$ | Hellier et al. (2014) | Andreasen et al. (2017) |  |

Table 1 （continued）
An Upper Bound on the Masses of Planets

| System |  | R．A． | Decl． | Mass | Metallicity | Discovery <br> Reference | Stellar Parameter <br> Reference |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Name |  |  |  |  |  |  |
|  |  | （ hms ） | （ dms ） | （ $M_{\text {Jup }}$ ） |  |  |  |
| WASP－12 | WASP－12 | 063032.7943 | ＋29 4020.287 | $1.35_{-0.06}^{+0.07}$ | ${ }_{0.21}{ }_{-0.04}^{+0.04}$ | Hebb et al．（2009） | Mortier et al．（2013b） |
| HAT－P－8 | HAT－P－8 | 225209.8629 | ＋35 2649.605 | $1.44{ }_{-0.15}^{+0.17}$ | $0.07{ }_{-0.04}^{+0.04}$ | Latham et al．（2009） | Mortier et al．（2013b） |
| OGLE－TR－056 | V＊V5157 Sgr | 175635.51 | －29 3221.2 | $1.44{ }_{-0.18}^{+0.19}$ | $0^{0.25}{ }_{-0.08}^{+0.08}$ | Konacki et al．（2003） | Santos et al．（2006） |
| WASP－72 | CD－30 1019 | 024409.6110 | －30 1008.570 | $1.45{ }_{-0.05}^{+0.06}$ | $0.15{ }_{-0.06}^{+0.06}$ | Gillon et al．（2013） | Andreasen et al．（2017） |
| WASP－50 | TYC 5290－462－1 | 025445.1351 | $-105353.037$ | ${ }_{1.51}{ }_{-0.09}^{+0.09}$ | $0.13{ }_{-0.03}^{+0.03}$ | Gillon et al．（2011） | Mortier et al．（2013b） |
| KOI－1257 | Kepler－420 | 192454.043 | ＋445538．58 | $1.55_{-0.37}^{+0.37}$ | $0_{0.22}^{+0.04}$ | Santerne et al．（2014） | Santerne et al．（2014） |
| WASP－5 | GSC 08018－00199 | 235723.759 | －41 1637.74 | $1.62{ }_{-0.10}^{+0.13}$ | $0.17{ }_{-0.06}^{+0.06}$ | Anderson et al．（2008） | Mortier et al．（2013b） |
| WASP－77 A | BD－07 436A | 022837.2266 | －07 0338.366 | $1.71{ }_{-0.06}^{+0.06}$ | $0^{0.07}{ }_{-0.03}^{+0.03}$ | Maxted et al．（2013） | Mortier et al．（2013b） |
| K2－34 | TYC 1391－121－1 | 083018.9080 | ＋22 1409.313 | $1.79{ }_{-0.13}^{+0.13}$ | $0_{0.11}{ }_{-0.04}^{+0.04}$ | Hirano et al．（2016） | Lillo－Box et al．（2016）品 |
| HAT－P－7 | BD＋47 2846 | 192859.3534 | ＋475810．229 | $1.81{ }_{-0.02}^{+0.02}$ | $0.31_{-0.07}^{+0.07}$ | Pál et al．（2008） | Ammler－von Eiff et al．（2009） |
| TrES－3 | NAME TrES－3b | 175207.020 | ＋37 3246.18 | $1.84{ }_{-0.08}^{+0.07}$ | $-_{-0.10}{ }_{-0.19}^{+0.19}$ | O＇Donovan et al．（2007） | Ammler－von Eiff et al．（2009） |
| WASP－100 | CPD－64 356 | 043550.3297 | －64 0137.316 | $1.87{ }_{-0.11}^{+0.11}$ | ${ }_{-0.30_{-0.12}^{+0.12}}$ | Hellier et al．（2014） | Andreasen et al．（2017）（2017） |
| WASP－73 | HD 202678 | 211947.9070 | －58 0855.951 | $1.87{ }_{-0.06}^{+0.07}$ | $0.20_{-0.02}^{+0.02}$ | Delrez et al．（2014） | Andreasen et al．（2017） |
| WASP－3 | TYC 2636－195－1 | 183431.6241 | ＋35 3941.488 | ${ }_{1.92}{ }_{-0.06}^{+0.06}$ | ${ }_{-0.02}^{+0.08}$ | Pollacco et al．（2008） | Montalto et al．（2012） |
| WASP－37 | GSC 00326－00658 | 144746.560 | ＋010353．85 | $1.93{ }_{-0.18}^{+0.18}$ | $-0.23_{-0.05}^{+0.05}$ | Simpson et al．（2011） | Andreasen et al．（2017） |
| HATS－1 | HATS－1 | 114206.080 | －23 2117.44 | $1.94{ }_{-0.21}^{+0.27}$ | ${ }_{-0.04}^{+0.04}$ | Penev et al．（2013） | Andreasen et al．（2017） |
| WASP－61 | TYC 6469－1972－1 | 050111.9193 | －2603 14．973 | $2.00_{-0.17}^{+0.17}$ | ${ }_{-0.38}^{+0.11}$ | Hellier et al．（2012） | Andreasen et al．（2017）O |
| HAT－P－23 | TYC 1632－1396－1 | 202429.7254 | ＋164543．812 | $2.11{ }_{-0.12}^{+0.12}$ | $0.16{ }_{-0.03}^{+0.03}$ | Bakos et al．（2011） | Tsantaki et al．（2014） |
| WASP－71 | TYC 30－116－1 | 015703.2070 | ＋00 4531.865 | $2.11{ }_{-0.08}^{+0.08}$ | $0.37{ }_{-0.04}^{+0.04}$ | Smith et al．（2013） | Mortier et al．（2013b） |
| HAT－P－14 | TYC 3086－152－1 | 172027.8775 | ＋38 1431.911 | $2.19{ }_{-0.06}^{+0.06}$ | $0^{0.17}{ }_{-0.07}^{+0.07}$ | Torres et al．（2010） | Sousa et al．（2015） |
| WASP－36 | GSC 05442－00759 | 084619.298 | －08 0137.01 | $2.24{ }_{-0.07}^{+0.07}$ | ${ }_{-0.01}+0.05$ | Smith et al．（2012） | Mortier et al．（2013b） |
| Kepler－17 | KOI－203 | 195334.866 | ＋474854．02 | $2.26{ }_{-0.10}^{+0.10}$ | $0.26{ }_{-0.10}^{+0.10}$ | Désert et al．（2011） | Bonomo et al．（2012） |
| WASP－8 | TYC 7522－505－1 | 235936.0711 | －35 0152.920 | $2.26{ }_{-0.09}^{+0.08}$ | $0.29{ }_{-0.03}^{+0.03}$ | Queloz et al．（2010） | Mortier et al．（2013b）［⿴囗十心夊 |
| HAT－P－22 | HD 233731 | 102243.5927 | ＋50 0742.060 | $2.37{ }_{-0.07}^{+0.07}$ | $0.28{ }_{-0.05}^{+0.05}$ | Bakos et al．（2011） | Sousa et al．（2015）O |
| WASP－66 | TYC 7193－1804－1 | 103253.9926 | $-345923.452$ | $2.43_{-0.14}^{+0.14}$ | $0.05{ }_{-0.05}^{+0.05}$ | Hellier et al．（2012） | Mortier et al．（2013b） |
| WASP－99 | CD－50 777 | 023935.4435 | $-500028.875$ | $2.46{ }_{-0.11}^{+0.11}$ | $0.27{ }_{-0.06}^{+0.06}$ | Hellier et al．（2014） | Andreasen et al．（2017） |
| Corot－10 | Corot－10 | 192415.296 | ＋00 4445.99 | $\begin{gathered} 2.56_{-0.15}^{+0.15} \end{gathered}$ | $0_{0.06}^{+0.09}$ | Bonomo et al．（2010） | Mortier et al．（2013b）号 |
| WASP－38 | HD 146389 | 161550.3646 | ＋10 0157.280 | $2.60_{-0.06}^{+0.06}$ | $0.06{ }_{-0.04}^{+0.04}$ | Barros et al．（2011） | Mortier et al．（2013b） |
| Corot－11 | CoRot－11 | 184244.947 | ＋05 5615.70 | $2.67{ }_{-0.39}^{+0.39}$ | $0.04{ }_{-0.03}^{+0.03}$ | Gandolfi et al．（2010） | Tsantaki et al．（2014） $\mathrm{S}^{\text {a }}$ |
| Qatar－2 | Qatar 2 | 135037.409 | －06 4814.41 | $2.80{ }_{-0.06}^{+0.06}$ | $0.09{ }_{-0.17}^{+0.17}$ | Bryan et al．（2012） | Andreasen et al．（2017） |
| Kepler－43 | Kepler－43 | 190057.810 | ＋464005．62 | $3.11{ }_{-0.25}^{+0.25}$ | $0.33{ }_{-0.11}^{+0.11}$ | Bonomo et al．（2012） | Bonomo et al．（2012） |
| HD 17156 | HD 17156 | 024944.4873 | ＋714511．630 | $3.13_{-0.08}^{+0.08}$ | $0.23{ }_{-0.04}^{+0.04}$ | Fischer et al．（2007） | Ammler－von Eiff et al．（2009） |
| WASP－10 | GSC 02752－00114 | 231558.299 | $+312746.28$ | $3.18{ }_{-0.11}^{+0.13}$ | $0.04{ }_{-0.05}^{+0.05}$ | Christian et al．（2009） | Mortier et al．（2013b） |
| HAT－P－34 | HD 351766 | 201246.8851 | ＋180617．431 | $3.28{ }_{-0.21}^{+0.21}$ | $0.08{ }_{-0.05}^{+0.05}$ | Bakos et al．（2012） | Tsantaki et al．（2014） |
| CoRot－2 | CoRot－2 | 192706.496 | ＋012301．38 | $3.30{ }_{-0.21}^{+0.21}$ | ${ }_{-0.09}{ }_{-0.07}^{+0.07}$ | Alonso et al．（2008） | Mortier et al．（2013b） |
| WASP－32 | TYC 2－1155－1 | 001550.8103 | ＋01 1201.592 | $3.88{ }_{-0.08}^{+0.08}$ | ${ }_{0.28}{ }_{-0.10}^{+0.10}$ | Maxted et al．（2010a） | Mortier et al．（2013b） |
| HD 80606 | HD 80606 | 092237.5769 | ＋50 3613.430 | ${ }_{4.02}{ }_{-0.11}^{+0.11}$ | $0.32{ }_{-0.09}^{+0.09}$ | Naef et al．（2001） | Santos et al．（2004） |
| HAT－P－20 | HAT－P－20 | 072739.950 | ＋24 2011.49 | $7.31{ }_{-0.19}^{+0.19}$ | $0.12_{-0.15}^{+0.15}$ | Bakos et al．（2011） | Mortier et al．（2013b） |
| HAT－P－2 | HD 147506 | 162036.3576 | ＋410253．107 | $9.00_{-0.24}^{+0.24}$ | $0.04{ }_{-0.05}^{+0.05}$ | Bakos et al．（2007a） | Tsantaki et al．（2014） |
| WASP－18 | HD 10069 | 013725.0332 | －454040．373 | $10.16{ }_{-0.37}^{+0.37}$ | $0.19{ }_{-0.05}^{+0.05}$ | Hellier et al．（2009a） | Mortier et al．（2013b） |
| XO－3 | TYC 3727－1064－1 | 042152.7053 | ＋57 4901.868 | $13.06_{-0.65}^{+0.65}$ | ${ }_{-0.08}^{+0.04}$ | Johns－Krull et al．（2008） | Tsantaki et al．（2014） |
| CoRoT－3 | CoRoT－3 | 192813.265 | ＋00 0718.62 | $22.08{ }_{-1.02}^{+1.02}$ | ${ }_{0.14}{ }_{-0.04}^{+0.04}$ | Deleuil et al．（2008） | Tsantaki et al．（2014） |

Table 2. Brown dwarfs and Low-mass Stars that have Doppler-inferred Masses and Transit Solar-type Stars

| System | Simbad | R.A. | Decl. | Mass | Metallicity | Discovery <br> Reference | Parameter <br> Reference ${ }^{\text {a }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Name |  |  |  |  |  |  |
|  |  | ( hms ) | ( dms ) | ( $M_{\text {Jup }}$ ) |  |  |  |
| Kepler-39 | KOI-423 | 194750.468 | +460203.43 | $20.1{ }_{-1.3}^{+1.2}$ | $0.1{ }_{-0.14}^{+0.14}$ | Bouchy et al. (2011a) | Bonomo et al. (2015) |
| KELT-1 | TYC 2785-2130-1 | 000126.9206 | +39 2301.773 | $27.37{ }_{-0.92}^{+0.92}$ | $0_{0.052}{ }_{-0.079}^{+0.079}$ | Siverd et al. (2012) |  |
| EPIC 219388192 | UCAC4 366-166973 | 191734.026 | -165217.75 | $36.5{ }_{-0.09}^{+0.09}$ | $0_{0.03}^{+0.08}$ | Curtis et al. (2016) | Nowak et al. (2017) |
| KOI-205 | KOI-205 | 194159.197 | +423216.40 | $40.8{ }_{-1.1}^{+1.5}$ | $0.18{ }_{-0.12}^{+0.12}$ | Díaz et al. (2013) | Bonomo et al. (2015) |
| CoRot-33 | 2MASS J18383391+0537287 | 183833.917 | +05 3728.77 | 59. ${ }_{-1.8}^{+1.7}$ | 0.44 ${ }_{-0.1}^{+0.1}$ | Csizmadia et al. (2015) |  |
| KOI-415 | KOI-415 | 193313.452 | +41 3622.94 | $62.14{ }_{-2.69}^{+2.69}$ | $-0.24_{-0.11}^{+0.11}$ | Moutou et al. (2013) |  |
| WASP-30 | WASP-30 | 235338.0552 | $-100705.107$ | $62.5{ }_{-1.2}^{+1.2}$ | $0.083_{-0.069}^{+0.05}$ | Anderson et al. (2011a) | Triaud et al. (2013) |
| CoRoT-15 | CoRot-15 | 062827.819 | +06 1110.54 | $63.3{ }_{-4.1}^{+4.1}$ | $0.1{ }_{-0.2}^{+0.2}$ | Bouchy et al. (2011b) |  |
| EPIC 201702477 | UCAC2 33047398 | 114057.792 | +03 4053.70 | $66.9{ }_{-1.7}^{+1.7}$ | $-^{0.164}{ }_{-0.053}^{+0.053}$ | Bayliss et al. (2017) |  |
| KOI-189 | KOI-189 | 185931.191 | +491601.18 | 78. ${ }_{-3.4}^{+3.4}$ | ${ }_{-0.115_{-0.099}^{+0.099}}$ | Díaz et al. (2014) |  |
| EbLM Jo555-57A | CD-57 1311 | 055532.6868 | -57 1726.064 | $85.2{ }_{-4}^{+3.9}$ | $-0.24{ }_{-0.16}^{+0.16}$ | von Boetticher et al. (2017) |  |
| TYC 7760-484-1 | CD-39 7570 | 121921.0385 | -39 5125.575 | $95.4{ }_{-1.9}^{+2.5}$ | ${ }_{-0.209}{ }_{-0.07}^{+0.075}$ | Triaud et al. (2013) |  |
| OGLE-TR-122 | V* V817 Car | 110651.89 | -60 5145.9 | 96. ${ }_{-9} 9$ | $0.15{ }_{-0.36}^{+0.36}$ | Pont et al. (2005) |  |
| 1SWASP J234318.41+295556.5 | BD+29 4980 | 234318.4125 | +2955 56.696 | 100. ${ }_{-7}^{+7}$ | $0.07{ }_{-0.008}^{+0.17}$ | Chaturvedi et al. (2016) |  |
| CoRot 101186644 | 2MASS J19265907+0029061 | 192659.078 | +00 2906.19 | 100. ${ }_{-12}^{+12}$ | $0.2_{-0.2}^{+0.2}$ | Tal-Or et al. (2013) |  |
| KOI-686 | KOI-686 | 194721.783 | +43 3849.64 | $103.4{ }_{-4.8}^{+4.8}$ | ${ }_{-0.06}{ }_{-0.13}^{+0.13}$ | Díaz et al. (2014) |  |
| HATS550-016 | GSC 06465-00602 | 044823.318 | -245016.88 | 115. ${ }_{-5}^{+6}$ | $-0.6{ }_{-0.06}^{+0.06}$ | Zhou et al. (2014) |  |
| HAT-TR-205-013 | NAME HAT-TR-205-013 | 230808.3420 | +33 3803.963 | 130. ${ }_{-10}^{+10}$ | ${ }_{-0.2}{ }_{-0.2}^{+0.2}$ | Beatty et al. (2007) |  |
| HATS551-021 | GSC 06493-00315 | 054249.120 | -25 5947.49 | 138. ${ }_{-15}^{+5}$ | $-0.4{ }_{-0.1}^{+0.1}$ | Zhou et al. (2014) |  |
| KIC 1571511 | KOI-362 | 192359.256 | +371157.19 | 150. ${ }_{-5}^{+4}$ | $0.37{ }_{-0.08}^{+0.08}$ | Ofir et al. (2012) |  |
| HATS551-019 | TYC 6493-290-1 | 054046.1695 | -24 5535.189 | 180. ${ }_{-10}^{+10}$ | ${ }_{-0.4}{ }_{-0.1}^{+0.1}$ | Zhou et al. (2014) |  |
| TYC 3700-1739-1 | TYC 3700-1739-1 | 024051.519 | +524506.27 | 197. ${ }_{-15}^{+15}$ | ${ }_{-0.05}^{+0.17}$ | Eigmüller et al. (2016) |  |
| T-Lyr1-01662 | TYC 3545-371-1 | 185902.8586 | +483635.557 | 207. ${ }_{-13}^{+13}$ | ${ }_{-0.5}{ }_{-0.2}^{+0.2}$ | Fernandez et al. (2009) |  |
| HATS553-001 | GSC 05946-00892 | 061600.656 | -21 1523.82 | 210. ${ }_{-10}^{+20}$ | $-0.1_{-0.2}^{+0.2}$ | Zhou et al. (2014) |  |
| Kepler-16 | Kepler-16 | 191618.175 | +514526.76 | $212.17{ }_{-0.69}^{+0.68}$ | ${ }_{-0.3}+0.2$ | Doyle et al. (2011) |  |
| T-Lyr0-08070 | TYC 3121-1659-1 | 191903.7120 | +384056.775 | 251. ${ }_{-20}$ | $-0.5{ }_{-0.2}^{+0.2}$ | Fernandez et al. (2009) |  |
| HD 213572 | HD 213572 | 223200.1305 | +271409.767 | 300. ${ }_{-13}^{+10}$ | ${ }_{-0.065}{ }_{-0.05}^{+0.048}$ | Chaturvedi et al. (2014) |  |

[^3]
[^0]:    1 The $p$-values produced by the Kolmogorov-Smirnov test are not generated by comparison with a Gaussian distribution, so I only give a numerical value of $\sigma$ to aid in the comparison of this result to those of previous studies.

[^1]:    ${ }^{2}$ See Baruteau et al. (2016) for a comprehensive review.

[^2]:    3 The frequent occurrence of low-mass stars in Doppler-selected samples of high-mass brown dwarfs has also been seen by Wilson et al. (2016).

[^3]:    ${ }^{a}$ Only included if it is different than the discovery reference.

